Moduli, a 0.1 – 1 keV Cosmic Axion Background and the Galaxy Cluster Soft Excess

Joseph Conlon, Oxford University

Strings 2014, Princeton, 23rd June 2014
1. Moduli

2. The Cosmological Moduli Problem

3. Dark Radiation

4. A 0.1 - 1 keV Cosmic Axion Background

5. Observing a Cosmic Axion Background and the Cluster Soft Excess
Thanks to my collaborators

1208.3562 Michele Cicoli, JC, Fernando Quevedo
‘Dark Radiation in LARGE Volume Models’

1304.1804 JC, David Marsh
‘The Cosmophenomenology of Axionic Dark Radiation’

1305.3603 JC, David Marsh
‘Searching for a 0.1-1 keV Cosmic Axion Background’

1312.3947 Stephen Angus, JC, David Marsh, Andrew Powell, Lukas Witkowski
‘Soft X-Ray Excess in the Coma Cluster from a Cosmic Axion Background’

1406.5188 David Kraljic, Markus Rummel, JC
‘ALP Conversion and the Soft X-Ray Excess in the Outskirts of the Coma Cluster’
I

MODULI
How to turn string compactifications into observational predictions?

It is difficult to single out any preferred extension of the Standard Model as there are so many different approaches to realising the Standard Model.

- Weakly coupled heterotic string
- Free fermionic models
- Rational CFT models (Gepner models)
- IIA intersecting D6 branes
- Branes at singularities
- M-theory on singular G2 manifolds
- IIB magnetised branes with fluxes
- F-theory
Instead more useful to focus on the most generic features of compactifications: the moduli sector.

Closed string sector always present and involves modes (dilaton / volume modulus) always present in compactified string theory.

Such extra-dimensional modes are necessarily present in the spectrum on compactification of 10d theory to four dimensions.

Much of the physics of moduli is universal across compactifications.
II
THE COSMOLOGICAL MODULI PROBLEM
The Standard Cosmology:

- inflationary expansion
- matter domination by inflaton quanta
- Decay of inflaton
- gg, qq, e+ e-, ......

Visible Sector Reheating

Joseph Conlon, Oxford University
Hot Big Bang starts when universe becomes radiation dominated. This occurs ‘when inflaton decays’. However:

- Non-relativistic matter redshifts as \( \rho_\Phi \sim a(t)^{-3} \)
- Radiation energy density redshifts as \( \rho_\gamma \sim a(t)^{-4} \)
- Therefore as \( a(t) \to \infty \), \( \frac{\rho_\gamma}{\rho_\Phi} \to 0 \)

Long-lived matter comes to dominate almost independent of the initial conditions.

Reheating is dominated by the LAST scalar to decay NOT the first.
Moduli are generically misaligned from their final minimum during inflation, and after inflation oscillate as non-relativistic matter ($\rho \sim a^{-3}$) before decaying.

Misalignment occurs as inflationary potential contributes to the moduli potential:

$$V_{\text{inf}} = V_{\text{inf}}(S, T, \ldots)$$

The closed string origin of moduli imply their interactions are ‘gravitational’ and suppressed by powers of $M_P$.

Moduli live a long time and come to dominate the energy density of the universe.
Lifetime of moduli is determined by $M_P$-suppressed decay rate:

$$\Gamma \sim \frac{1}{8\pi} \frac{m^3}{M_P^2}$$

$$\tau = \Gamma^{-1} \sim 8\pi \frac{M_P^2}{m^3} = \left( \frac{100\text{TeV}}{m_\Phi} \right)^3 0.1\text{s}$$

$$T_{\text{decay}} \sim \left( \frac{m_\Phi}{100\text{TeV}} \right)^{3/2} 3\text{ MeV}$$

Hot Big Bang does not start until moduli decay.

The cosmological moduli problem is the statement that for $m_\Phi \lesssim 100\text{TeV}$ moduli decays spoil predictions of big bang nucleosynthesis.

Side consequence: generic expectation of string compactifications is that the universe passes through a modulus-dominated epoch, and reheating comes from the decays of these moduli.
We expect reheating to be driven by the late-time decays of massive Planck-coupled particles.

Last decaying scalar

\[ \Phi \]

\[ gg, qq, e^+ e^-, \ldots \]

\[ \text{VISIBLE SECTOR REHEATING} \]

\[ aa \]

\[ \text{DARK RADIATION} \]

Hidden sector decays of moduli give rise to dark radiation. Ideal subject for string phenomenology!
The Cosmological Moduli Opportunity

- Inflationary expansion
- Matter domination by inflaton quanta
- Oscillations and reheating
- Decay of inflaton
  - gg, qq, e+ e-, ......
  - aa

Joseph Conlon, Oxford University

Moduli, a 0.1 – 1 keV Cosmic Axion Background and the Galaxy
As gravitationally coupled particles, moduli generally couple to everything with $M_P^{-1}$ couplings and there is no reason to expect vanishing couplings to hidden sectors.

Visible sector: \[
\frac{\Phi}{4M_P} F_{\mu\nu}^{\text{color}} F_{\mu\nu}^{\text{color}}, \quad \frac{\partial_\mu \partial^\mu \Phi}{M_P} H_u H_d, \ldots
\]

Hidden sector: \[
\frac{\Phi}{2M_P} \partial_\mu a \partial^\mu a, \quad \frac{\Phi}{4M_P} F_{\mu\nu}^{\text{hidden}} F_{\mu\nu}^{\text{hidden}}, \ldots
\]

This is supported by explicit studies of string effective field theories.

In particular, axionic decay modes naturally arise with

$$\text{BR}(\Phi \rightarrow aa) \sim 0.01 \rightarrow 1.$$
Independent of susy breaking scale in string models reheating is driven by decays of the lightest moduli, and dark radiation arises from hidden sector decays of these moduli.

Example: volume modulus in LVS, $\tau_b$ is lightest moduli and has a massless volume axion partner $a_b$

$$K = -3 \ln \left( T_b + \bar{T}_b \right)$$

$$\mathcal{L} = \frac{3 \partial_\mu \tau_b \partial^\mu \tau_b}{4 \tau_b^2} + \frac{3 \partial_\mu a_b \partial^\mu a_b}{4 \tau_b^2}$$

Volume modulus $\tau_b$ has hidden sector decay $\tau_b \rightarrow a_b a_b$ to volume axion. 1208.3562 Cicoli JC Quevedo 1208.3563 Higaki Takahashi

What happens to $a_b$? It becomes Dark Radiation
III

DARK RADIATION
Both the CMB and primordial BBN abundances are sensitive to additional dark radiation in the early universe (which changes the expansion rate).

In the CMB, $\Delta N_{\text{eff}}$ modifies the damping tail of the CMB and is probed by the ratio between the damping scale and the sound horizon.

At BBN times, extra radiation modifies the expansion rate at a given temperature.

This affects the primordial Helium and Deuterium abundances: $(D/H)_p$ (where $N_{\text{eff}}$ is degenerate with $\Omega_b h^2$) and $Y_p$.

Recent observations have tended to hint at the $1 \div 3\sigma$ level for $\Delta N_{\text{eff}} > 0$. 
Various (non-independent) recent measurements, 1 \( \sigma \) error bars:

- **CMB + BAO**
  - \( 3.55 \pm 0.60 \) (WMAP9 + eCMB + BAO, 1212.5226)
  - \( 3.50 \pm 0.47 \) (SPT + CMB + BAO, 1212.6267)
  - \( 2.87 \pm 0.60 \) (WMAP7 + ACT + BAO, 1301.0824)
  - \( 3.30 \pm 0.27 \) (Planck + eCMB + BAO, 1303.5076)

- **CMB + BAO + \( H_0 \)**
  - \( 3.84 \pm 0.40 \) (WMAP9 + eCMB + BAO + H0, 1212.5226)
  - \( 3.71 \pm 0.35 \) (SPT + CMB + BAO + H0, 1212.6267)
  - \( 3.52 \pm 0.39 \) (WMAP7 + ACT + BAO+ H0, 1301.0824)
  - \( 3.52 \pm 0.24 \) (Planck + eCMB + BAO + H0, 1303.5076)

Expect significant improvement over next few years.
An independent probe of $N_{\text{eff}}$ is via BBN primordial abundances - new determinations of $Y_p$ and $(D/H)_P$ appeared recently.

\[
Y_p = 0.254 \pm 0.003 \quad (1308.2100, \text{Izotov et al})
\]
\[
(D/H)_P = (2.53 \pm 0.04) \times 10^{-5} \quad (1308.3240, \text{Cooke et al})
\]

Updated bounds: $(D/H)_P + \text{CMB}$

\[
N_{\text{eff}} = 3.28 \pm 0.28 \quad (\text{updates } 3.02 \pm 0.27 \text{ from Planck XVI})
\]

BBN alone $(D/H)_P + Y_p$: 

\[
N_{\text{eff}} = 3.50 \pm 0.20 \quad (1308.3240, \text{Cooke et al})
\]
IV
A COSMIC AXION BACKGROUND
A Cosmic Axion Background

String theory says we expect reheating to be driven by the late-time decays of massive Planck-coupled particles.

Last decaying scalar

```
Φ
```

- gg, qq, e+ e-, ......
- aa

**VISIBLE SECTOR REHEATING**

**DARK RADIATION**

Dark radiation arises from hidden sector decays of moduli

Ideal subject for string phenomenology!
Typical moduli couplings $\frac{\Phi}{4M_P} F_{\mu\nu} F^{\mu\nu}$ or $\frac{\Phi}{M_P} \partial_\mu a \partial^\mu a$ give

$$H_{\text{decay}} \sim \Gamma \sim \frac{1}{8\pi} \frac{m_\Phi^3}{M_P^2}$$

$$T_{\text{reheat}} \sim \left(3H_{\text{decay}}^2 M_P^2\right)^{1/4} \sim \frac{m_\phi^{3/2}}{M_P^{1/2}} \sim 0.6\text{GeV} \left(\frac{m_\phi}{10^6\text{GeV}}\right)^{3/2}$$

$$E_{\text{axion}} = \left(\frac{m_\phi}{2}\right) = 5 \times 10^5\text{GeV} \left(\frac{m_\phi}{10^6\text{GeV}}\right)$$

Visible sector thermalises: however axions propagate freely as universe is transparent to them.
A Cosmic Axion Background

Decay of inflaton

$\Phi$

gg, qq, e+ e-, ......

VISIBLE SECTOR

aa

DARK RADIATION

THERMALISED

FREE STREAMING
A Cosmic Axion Background

\[ \Phi \rightarrow gg, \ldots : \quad \text{Decays thermalise} \quad T_\gamma \sim T_{\text{reheat}} \sim \frac{m_\Phi^{3/2}}{M_P^2} \]

\[ \Phi \rightarrow aa : \quad \text{Axions never thermalise} \quad E_a = \frac{m_\Phi}{2} \]

Thermal bath cools into the CMB while axions never thermalise and freestream to the present day:
Ratio of axion energy to photon temperature is

\[ \frac{E_a}{T_\gamma} \sim \left( \frac{M_P}{m_\Phi} \right)^{1/2} \sim 10^6 \left( \frac{10^6 \text{GeV}}{m_\Phi} \right)^{1/2} \]

Retained through cosmic history!
A Cosmic Axion Background

Ratio of axion energy to photon temperature is

\[ \frac{E_a}{T_\gamma} \sim \left( \frac{M_P}{m_\Phi} \right)^{\frac{1}{2}} \sim 10^6 \left( \frac{10^6 \text{GeV}}{m_\Phi} \right)^{\frac{1}{2}} \]

No absolute prediction, but a lightest modulus mass \( m \sim 10^6 \text{GeV} \) arises in many string models - often correlated with SUSY approaches to the weak hierarchy problem.

- KKLT hep-th/0503216 Choi et al
- Sequestered LVS 0906.3297 Blumenhagen et al
- ‘G2 MSSM’ 0804.0863 Acharya et al

NB Moduli problem requires \( m_\Phi \gtrsim 10^5 \text{TeV} \).
Axions originate at $z \sim 10^{12}(t \sim 10^{-6}\text{ s})$ and freestream to today.

**PREDICTION: Cosmic Axion Background**

Energy: $E \sim 0.1 \div 1\text{keV}$  
Flux: $\sim \left( \frac{\Delta N_{\text{eff}}}{0.57} \right) 10^6\text{cm}^{-2}\text{s}^{-1}$. 

---

**Figure:**

A graph showing the energy distribution of cosmic axions, with the abscissa representing energy in eV and the ordinate representing the flux density in $10^3\text{cm}^{-2}\text{s}^{-1}\text{eV}^{-1}$. The peak flux density is observed around $E \sim 200\text{eV}$.
The current energy of such axionic dark radiation is

\[ E_a \sim 200\text{eV} \left( \frac{10^6 \text{GeV}}{m_\Phi} \right)^{\frac{1}{2}} \]

The expectation that there is a dark analogue of the CMB at \( E \gg T_{CMB} \) comes from very simple and general properties of moduli.

It is not tied to any precise model for moduli stabilisation, or approach to realising the Standard Model.

It just requires the existence of massive particles only interacting gravitationally.

For \( 10^5 \text{GeV} \lesssim m_\Phi \lesssim 10^8 \text{GeV} \) CAB lies today in extreme ultraviolet /soft X-ray wavebands.
V OBSERVING A COSMIC AXION BACKGROUND
How to see a CAB with $E_a \sim 0.1 - 1 \text{keV}$?

Axion-photon conversions come from axion coupling to electromagnetism:

$$\mathcal{L}_{a-\gamma} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{4M} a F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \partial_\mu a \partial^\mu a - \frac{1}{2} m_a^2 a^2.$$  

For general axion-like particles $M \equiv g_{a\gamma\gamma}^{-1}$ and $m_a$ are unspecified.  
We take $m_a = 0$ (in practice $\lesssim 10^{-12} \text{eV}$) and keep $M$ free.  
Direct bounds (axion production in supernovae) are $M \gtrsim 10^{11} \text{GeV}$.  

Joseph Conlon, Oxford University
Axion-to-photon conversion probability for axion energy $E_a$ in transverse magnetic field $B_\perp$ of domain size $L$ is:

$$P(a \rightarrow \gamma) = \sin^2(2\theta) \sin^2 \left( \frac{\Delta}{\cos 2\theta} \right)$$

where

$$\theta \approx 2.8 \cdot 10^{-5} \times \left( \frac{10^{-3} \text{cm}^{-3}}{n_e} \right) \left( \frac{B_\perp}{1 \mu\text{G}} \right) \left( \frac{E_a}{200 \text{ eV}} \right) \left( \frac{10^{14} \text{ GeV}}{M} \right),$$

$$\Delta = 0.27 \times \left( \frac{n_e}{10^{-3} \text{cm}^{-3}} \right) \left( \frac{200 \text{ eV}}{E_a} \right) \left( \frac{L}{1 \text{ kpc}} \right).$$
Axions convert to photons in coherent magnetic field domain: want large magnetic fields supported over large volumes.

Best locations are galaxy clusters:

- The largest virialised structures in the universe
- Typical size 1 Mpc, typical mass $10^{14} \div 10^{15} M_{\text{sun}}$.
- Large magnetic fields $B \sim 1 \div 10 \mu\text{G}$ coherent over $L \sim 1 \div 10$ kpc.
- Hot intracluster gas, $T_{\text{gas}} \sim 2 \div 10$ keV.
- By mass 1 per cent galaxies, 10 per cent gas, 90 per cent dark matter.
- Sit at the ‘large magnetic fields over large volumes’ frontier of particle physics.
The Coma Cluster in IR/Visible

Joseph Conlon, Oxford University
In fact there exists a long-standing (since 1996) EUV/soft x-ray excess from galaxy clusters (Lieu 1996, review Durret 2008). E.g Coma has

\[ \mathcal{L}_{\text{excess}} \sim 10^{43} \text{erg s}^{-1} \]

Observed by different satellites - principally EUVE and soft bands of ROSAT.

Has been studied for a large number (~ 40) of clusters, present in ~ 15.

Difficulties with astrophysical explanations - see backup slides.
The Cluster Soft Excess

from Bonamente et al 2002, fractional soft excess in ROSAT 0.14 – 0.28 keV R2 band
The Cluster Soft Excess

from Bonamente et al 2002, fractional soft excess with radius
The Cluster Soft Excess: Coma

Soft excess extends well beyond hot gas and cluster virial radius:

![Graph showing the relationship between distance and R2 band excess with S/N ratio] from 0903.3067 Bonamente et al, ROSAT R2 band (0.14-0.28keV) observations of Coma
The Cluster Soft Excess and a CAB

Proposal: cluster soft excess generated by $a \rightarrow \gamma$ conversion in cluster magnetic field.

Basic predictions:

- Magnitude and morphology of soft excess fully determined by cluster magnetic field and electron density
- Spatial extent of excess conterminous with magnetic field
- No thermal emission lines (e.g. O\textsubscript{VII}) associated to excess
- Energy of excess is constant across clusters, varying with redshift as $E_a \sim (1 + z)$.

Test by propagating axions through simulated cluster magnetic fields
Magnetic field model is best fit to Faraday rotation (Bonafede et al 1002.0594):

- Magnetic field has Kolmogorov spectrum, $|B(k)| \sim k^{-11/3}$, generated between $k_{max} = \frac{2\pi}{2\text{kpc}}$ and $k_{min} = \frac{2\pi}{34\text{kpc}}$.
- Spatial magnetic field has Gaussian statistics.
- Central magnetic field $\langle B \rangle_{r<291\text{kpc}} = 4.7 \mu\text{G}$
- Equipartition radial scaling of $B$, $B(r) \sim n_e(r)^{1/2}$
- Electron density taken from $\beta$-model with $\beta = 0.75$,

$$n_e(r) = 3.44 \times 10^{-3} \left(1 + \left(\frac{r}{291\text{kpc}}\right)^2\right)^{-\frac{3\beta}{2}} \text{cm}^{-3}$$

- Numerical $2000^3$ magnetic field with $0.5\text{kpc}$ resolution.

Numerical propagation of axions with $E = 25\text{eV} \div 25000\text{eV}$ and determination of $P(a \rightarrow \gamma)$. 

Joseph Conlon, Oxford University
Axion Propagation through Centre of Coma

\[ \langle P_{a\gamma} \rangle \ [10^{-4}] \]

Impact parameter [kpc]

\[ \begin{align*}
1 \text{ keV} & \\
600 \text{ eV} & \\
400 \text{ eV} & \\
200 \text{ eV} & \\
150 \text{ eV} & \\
100 \text{ eV} & \\
50 \text{ eV} & \\
25 \text{ eV} & 
\end{align*} \]

\( a \rightarrow \gamma \) conversion probabilities for different axion energies as a function of radius from the centre of Coma

Note the high suppression for \( E_a < 100 \text{eV} \)

Angus JC Marsh Powell Witkowski 1312.3947
Axion Propagation through Centre of Coma

Comparison of original axion spectrum and spectrum of converted photons

Photon spectrum falls off rapidly at both low and high energies
Morphology fits reasonably well for $M \sim 7 \times 10^{12}\text{GeV}$
Fit to the outskirts gives a compatible value of $M \sim 10^{13}\text{GeV}$.

Kraljic, Rummel, JC 1406.5188
Axion Propagation through Other Clusters

(Plots assume the Coma best fit value of $M \sim 7 \times 10^{12}\text{GeV}$)

Powell, to appear
Conclusions

- Physics of moduli suggests the existence of a Cosmic Axion Background with energies $E_a \gg T_{CMB}$
- CAB arises from hidden sectors decays of moduli to axions at the time of reheating
- CAB contributes to dark radiation and $\Delta N_{\text{eff}}$
- CAB energy today is naturally in $0.1 - 1 \text{ keV}$ range
- Axions can convert into photons in astrophysical magnetic fields, and CAB may be responsible for long-standing soft X-ray excess from galaxy clusters
BACKUP SLIDES
Two main proposals for astrophysical explanations:

1. A warm thermal gas with $T \sim 0.2\text{keV}$.
   Interpret soft excess as thermal bremsstrahlung emission from this warm gas.

2. A large non-thermal relativistic electron population with $E \sim 200 – 300 \text{MeV}$.
   Interpret soft excess as inverse Compton scattering of electrons on CMB.

Both have problems (in back-up slides).
The original proposal. However:

1. Such a gas is pressure unstable against the hot ICM gas. It rapidly cools away on a timescale much shorter than cluster timescales.

2. A thermal $T \sim 0.2\text{keV}$ gas would also have thermal emission lines - particularly O$_{VII}$ at 560 eV. No such lines have been observed - some early claimed detections have gone away.
A more promising proposal: a large population of non-thermal electrons scattering off the CMB. However:

1. If this population continues to $E \sim 2\text{GeV}$, its synchrotron radio emission is above level of Coma radio halo. This necessitates a sharp spectral cutoff between $\sim 200\text{MeV}$ and $\sim 2\text{GeV}$.

2. This population necessarily produces gamma rays through non-thermal bremsstrahlung.

It was predicted that these gamma rays would be easily observable by Fermi (Atoyan + Volk 2000)

But - Fermi does not see any clusters:

$$\mathcal{F}^{\text{Coma}}_{>100\ \text{MeV}} < 1.1 \times 10^{-9}\ \text{ph cm}^{-2} \ \text{s}^{-1}$$
Fig. 6.—Expected $\gamma$-ray fluxes expected from the Coma Cluster. The

from Atoyan + Volk, 2000
Coma in Gamma Rays

(Ando + Zandanel, 1312.1493)